
Program Logics

MAP-i – Proposal for the *Theory and Foundations* block, 2021-22

1 Context and Objectives

This document describes a proposal for a course on *Theory and Foundations* block to be offered in the 2021-22 MAP-i edition. The proposal is supported by a team from Aveiro University (Dep. of Mathematics) and Minho University (Dep. of Informatics).

The adoption of formal logics to modelling, design, implement and verify software is currently a well established practice. This course intends to make an overview on the topic, from the classic frameworks to imperative programs – Hoare and Dynamic Logics, to its current variants, prepared to aid the development of other less conventional computational domains as weighted, hybrid and quantum computations. The theoretical presentation of the topics will be enriched with a tools support component.

The course builds on the team previous research on program semantics and logics in software development, the latter object of the following research projects that have been (or currently are) coordinated by the proponents:

- NASONI (PTDC/EEI-CTP/2341/2012) on *Heterogenous software coordination: Foundations, methods, tools.*
- DALÍ (POCI-01-0145-FEDER-016692) on *Dynamic Logics for cyber-physical systems.*
- KLEE (POCI-01-0145-FEDER-030947) on *Coalgebraic Modeling and Analysis for Computational Synthetic Biology.*
- AVIACC (PTDC/EIA-CC0/117590/2010) on *Logic-based Analysis and Verification of Critical Concurrent Programs.*

2 Learning outcomes

- Take contact with formal logic, with a special focus in modal and dynamic logic.
- Take contact with the foundations of software verification, including Floyd-Hoare deductive verification and the corresponding bridge with dynamic logic
- To learn the principles of the formal verification of software
- Take contact with some computational tools to aid the formal specification and verification of software, including SMT solvers and other platforms for deductive proofs

3 Pre-requisites

The course is almost self-contained, assuming only familiarity with elementary discrete mathematics at MSc level.

4 Format

Tutorial module.

5 Grading

Assessment is based on an individual report on a research topic, and a small programming exercise in Why3.

6 Course Contents

M1-Introduction to formal logic (Manuel A. Martins)

- Propositional Logic – Syntax and Semantics, Formal deducibility, Completeness.
- First-Order Logic – Syntax and Semantics, Logical Consequence, Formal deducibility, Completeness.
- Modal Logic – Syntax, Kripke Semantics, Decidability, Completeness.

M2-Principles of SMT solving (Maria J. Frade)

- Overview of SMT solving technologies
- SMT solvers: logics and theories, pragmatic features, and encoding problems

M3-Logics for verification of classic programs (Alexandre Madeira)

- Preliminaries – programs relational semantics and the Kleene Algebra of programs
- Propositional Dynamic Logic
- Equational Dynamic Logic
- Introduction to axiomatic verification of programs – Floyd-Hoare Logic and Dijkstra transformations

M4-Tools support (Jorge S. Pinto)

- Introduction to the logic and program verification levels of the Why3 tool:
 - The logic language and the WhyML programming language
 - The Why3 IDE; prover interfacing and proof transformations; inductive proofs
- Program development and specification based on contracts
- Verification of functional and imperative programs with Why3

M5-Logics for the verification of weighted programs (Leandro Gomes)

- Multi-valued Propositional Dynamic Logic
- Multi-valued Equational Dynamic Logic
- Fuzzy programs as a special case: introducing semantics and logics

M6-Advanced topics

- Quantum dynamic logics (Luis S. Barbosa)
- Logics for Hybrid Systems (Renato Neves)
- Principles of SMT solving (Maria J. Frade)

7 Bibliography

M1 - Introduction to formal logic [Bur98, Gol87]

M2 - Principles of SMT solving [BHvMW09, BM07]

M3 - Logics for the verification of standard programs: [HKT00, AFPdS11, Dij76]

M4 - Tools support: [AFpdS11, FP13]

M5 - Logics for the verification of weighted programs [MNM16, GMJB19, Zad65, NW05]

8 Team

Alexandre Madeira (coordinator) is Assistant Professor at Department of Mathematics of Aveiro University and a researcher at CIDMA. He was a former MAP-i doctoral student. His PhD thesis on hybrid logic and software reconfiguration was later awarded the IBM Scientific Prize for 2013. He coordinated an FCT project, and he has published more than thirty papers in several journals and conferences over the past 5 years.

Selected relevant publications: [MNBM16, MBHM18, HMW18].

Manuel António Martins is Associated Professor of Mathematics Department of University of Aveiro, and a researcher at the Center for Research and Development in Mathematics and Applications (CIDMA). His research interests are related to Abstract Algebraic Logic, Modal Logic and Formal Methods. Namely, in what concerns the theoretical study of extensions of modal logics, over different paradigms such as fuzzy and paraconsistent ones, worth to reasoning about specific kinds of software systems. He participated in FCT-projects in themes related to the contents of this course. Currently, he is Co-PI of the Klee project, a project that aims to apply cyber-physical techniques to biological systems. He has published more than 25 papers in international journals and several in reviewed proceedings of relevant conferences in Computer Science. He has supervised 1 post-doc, 4 PhD and 10 MSc thesis.

Selected relevant publications: [CM17, BMMH19, MMH19, CFM20].

Maria João Frade is Assistant Professor of Informatics Department of University of Minho, and a member of the High Assurance Software Laboratory (HASLab) of INESC TEC. She received the PhD degree in computer science in 2004 from the University of Minho. In the past she worked on type theory, structural proof theory and type-systematic description of program analyses. In the last years her work focused on deductive program verification. She is one of the authors of a textbook in this area and published several papers in conferences and journals. *Selected relevant publications:* [LFP16a, FP11, AFPdS11].

Jorge Sousa Pinto is an Associate Professor at the Informatics Department of the University of Minho. He obtained his degree of Docteur de L'Ecole Polytechnique (Paris) in 2001 and his Habilitation from the University of Minho in 2015. In the past he has worked on linear logic and functional programming; more recently his work focused on deductive program verification. He is one of the authors of the textbook “Rigorous Software Development: an Introduction to Program Verification”. He is currently the director of the MAP-i doctoral programme.

Selected relevant publications: [LFP16b, eSAB⁺16, dMPPPP18].

Leandro Gomes is a researcher at INESC-TEC (HASLab) and team member of the FCT-funded research projects DaLí, Klee and Da Vinci. His research, most of it developed in the context of the referred projects, has been centred on semantics and program logics for weighted imperative programs. He has published some relevant publications in the last five years, including one in an international conference awarded with “Best Paper Award”.

Selected relevant publications: [GMB17, GMB19, GMJB19].

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